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# Determination of equivalent circuit models for the aggregated representation of downstream HV networks

Academia-Industry Workshop

Challenges of harmonic studies in modern transmission systems

TUD Dresden University of Technology

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# Agenda

- Motivation
- Downstream HV networks
- Equivalent circuit models
  - Circuit parameters
  - Circuit topologies
  - Application results
- Challenges

# Motivation

- Coordination and limitation of harmonic emissions for installations require **harmonic simulations** (to determine harmonic propagation (influence coefficients) and summation in transmission systems)
- Simulations based on **reliable models** of all relevant components, incl. **downstream distribution networks**
- Models of component require realistic **frequency-dependent impedances**



- **Implementation** of frequency-dependent impedances of **in simulations**
- **Determination of equivalent circuit models**  
for the aggregated representation of downstream HV networks

# Downstream HV networks

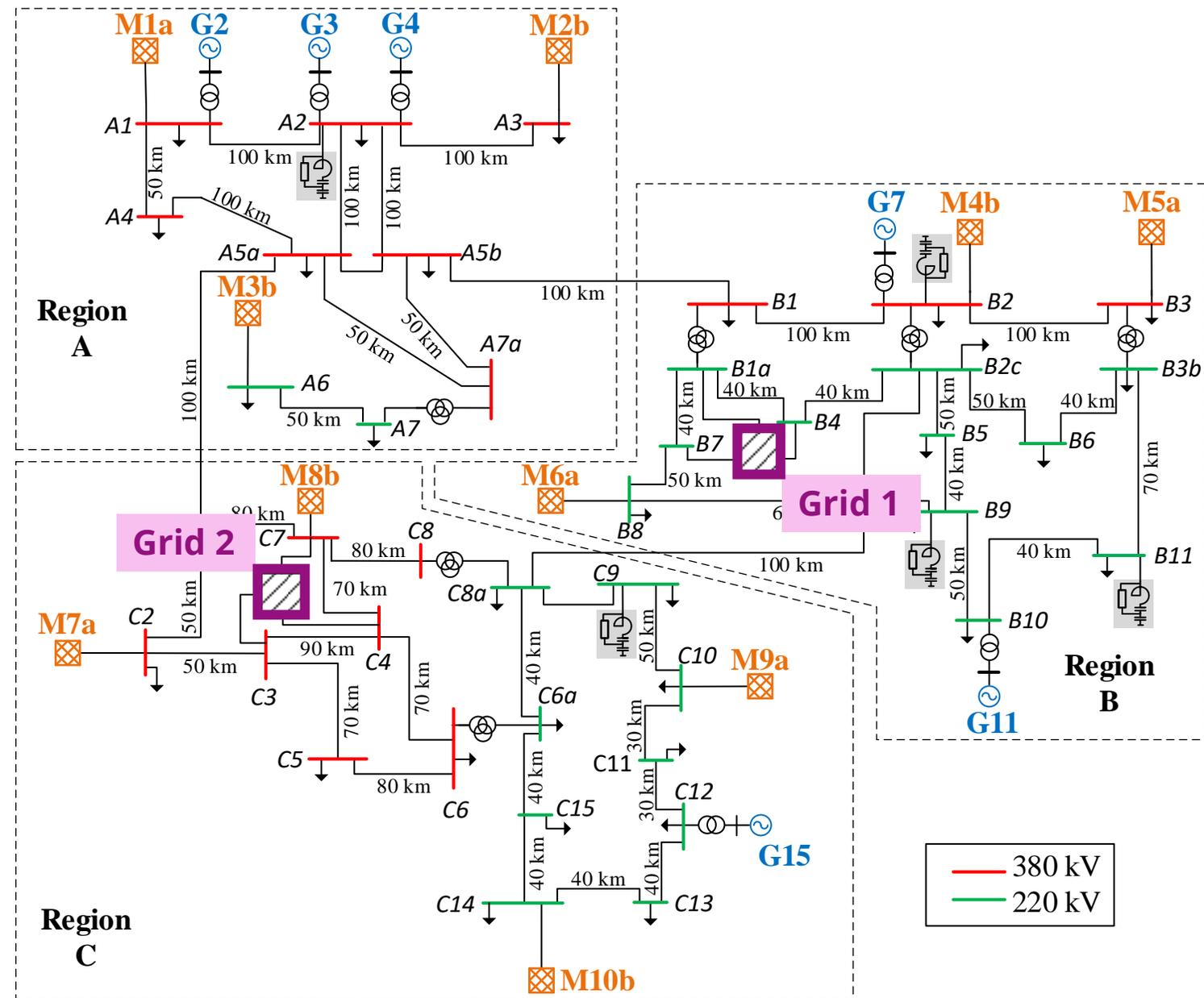
## Test network

### Transmission system

- 17 Nodes in 380 kV
- 22 Nodes in 220 kV
- 16 Generators (60% MMCs)
- 5 compensation devices

### Distribution system

- 39 Nodes in 110 kV
  - 37 aggregated networks
  - **2 detailed networks (with 3 in-feeds)**



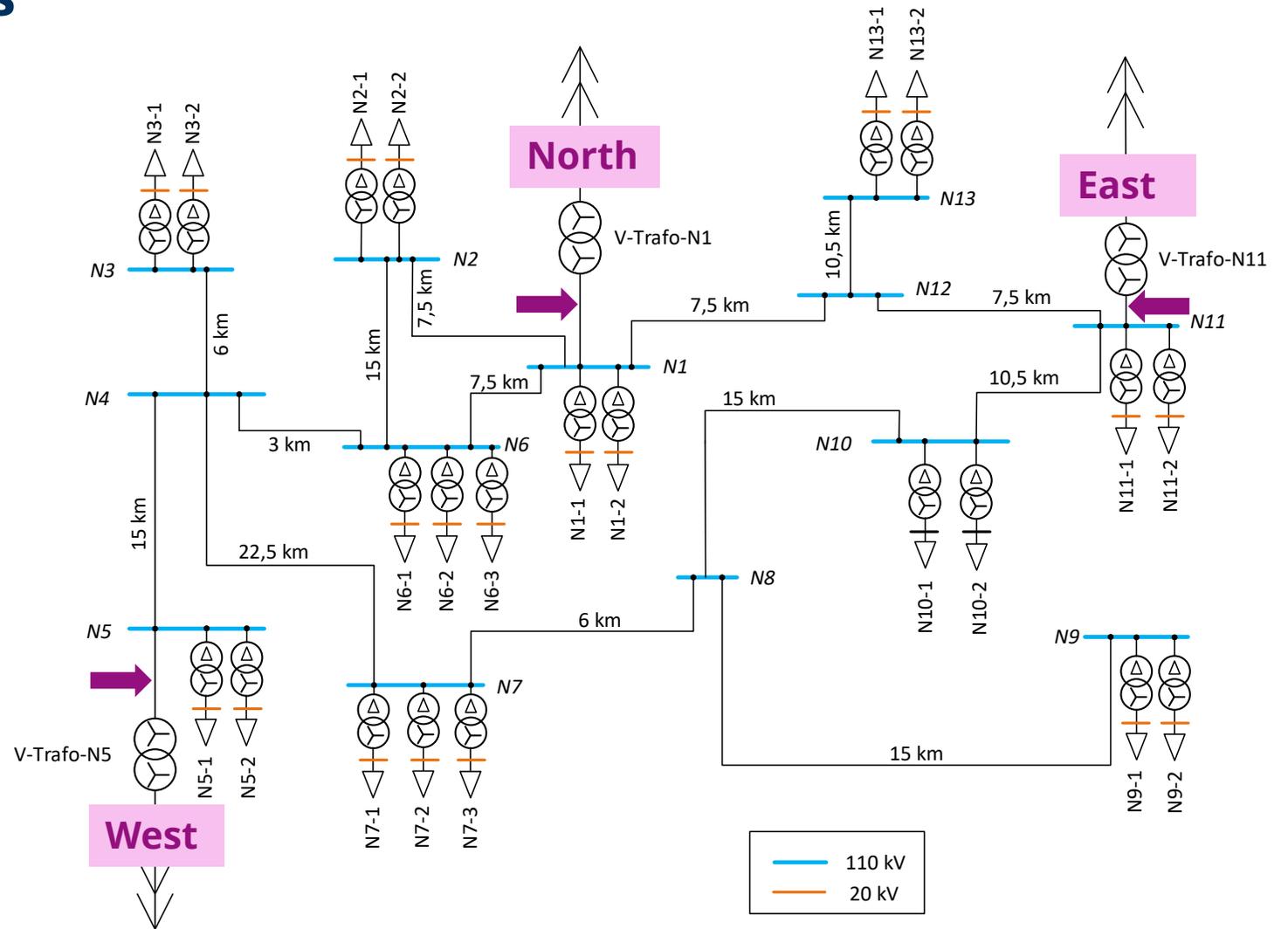
# Downstream HV networks

## Detailed 110-kV-model

### Model details

- 13 Nodes in 110 kV
- 22 Nodes in 20 kV
- Aggregated 20-kV-load models
- All overhead lines
- 3 in-feeds from EHV:
  - 220 kV for Grid 1
  - 380 kV for Grid 2

➤ **Determination of frequency-dependent downstream impedances of HV networks**

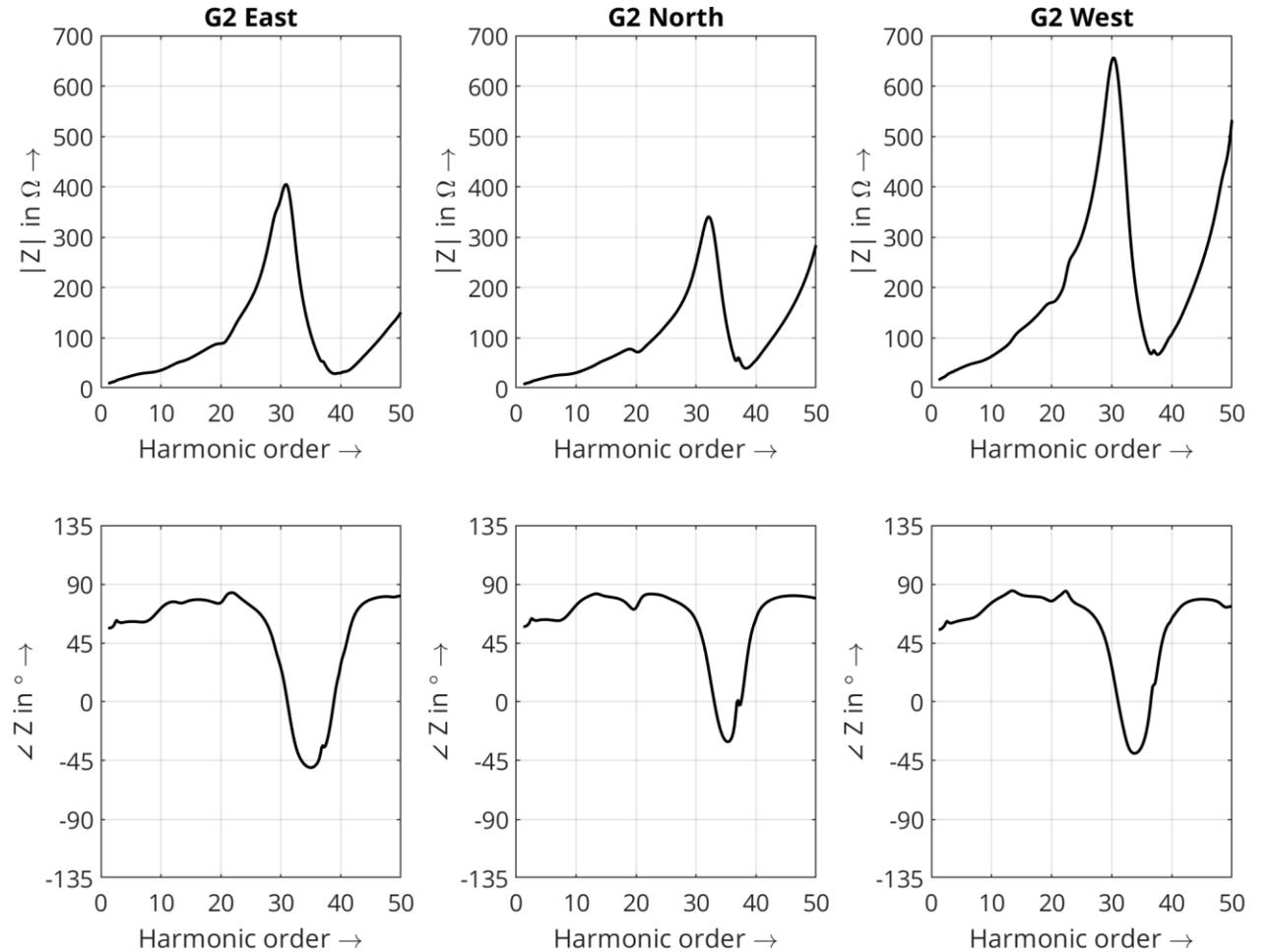


# Downstream HV networks

## Impedance characteristics (1)

- Focus on **positive sequence** impedances
- Multiple resonances for downstream impedance of detailed 110-kV-model
- Similar resonance frequencies at in-feeds

*Downstream HV impedance  
(at 110-kV-side of Grid 2)*



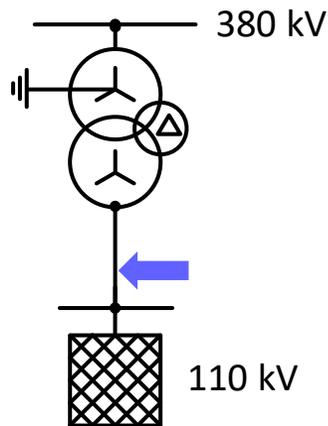
# Downstream HV networks

## Impedance characteristics (2)

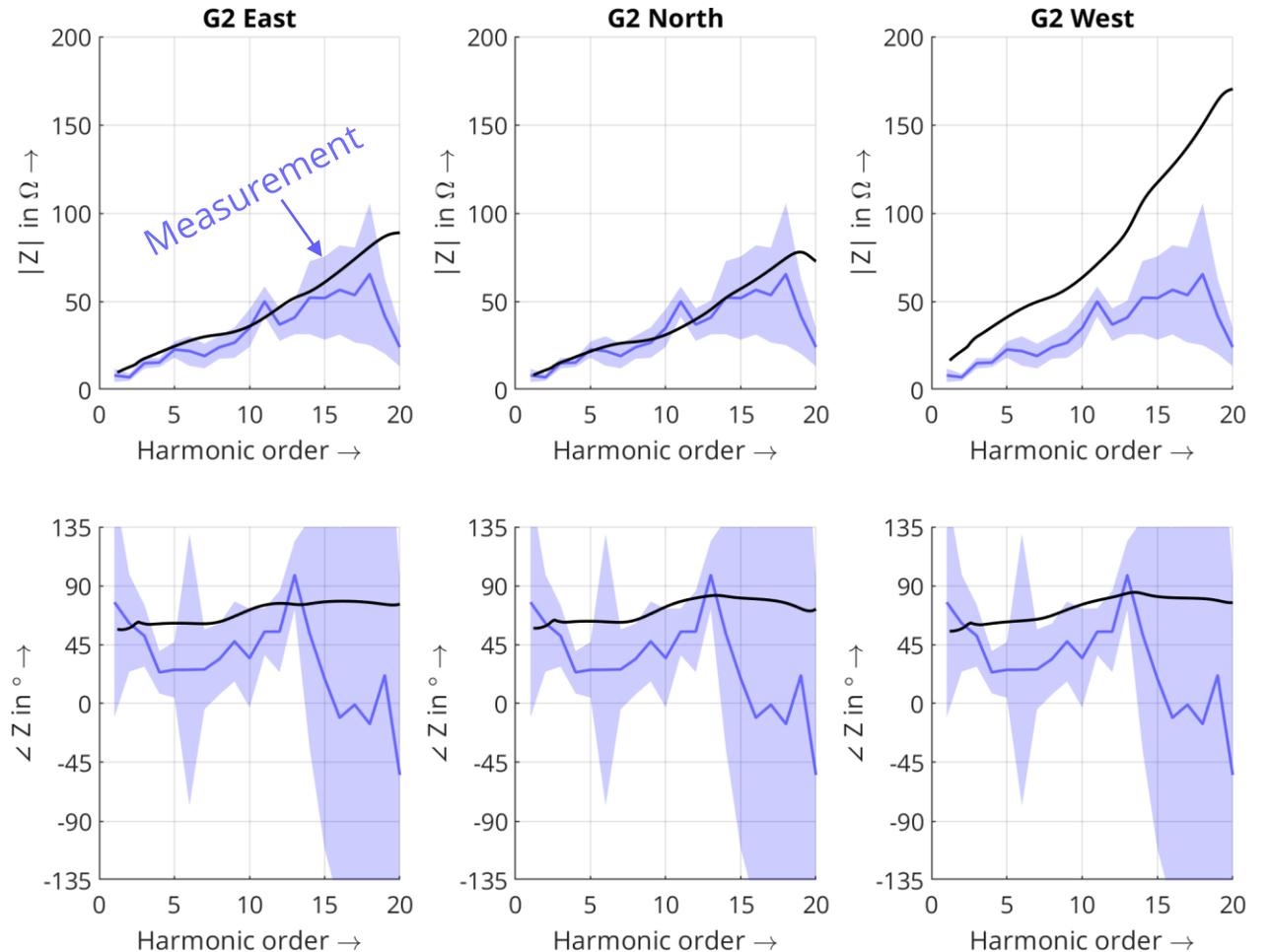
- Focus on **positive sequence** impedances
- Multiple resonances for downstream impedance of detailed 110-kV-model
- Similar resonance frequencies at in-feeds

### Field measurement:

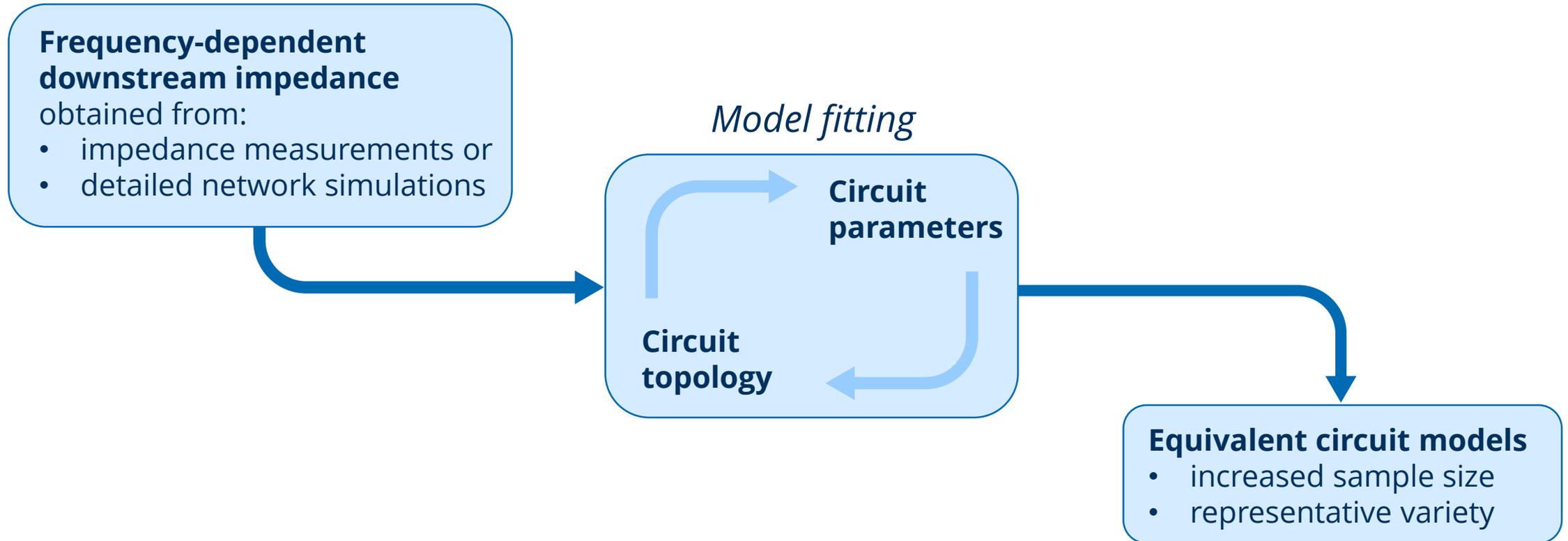
- Different network topology
- Excitation using transformer in-rush currents at 380 kV
- Comparable impedances



### Downstream HV impedance (at 110-kV-side of Grid 2)



# Equivalent circuit models

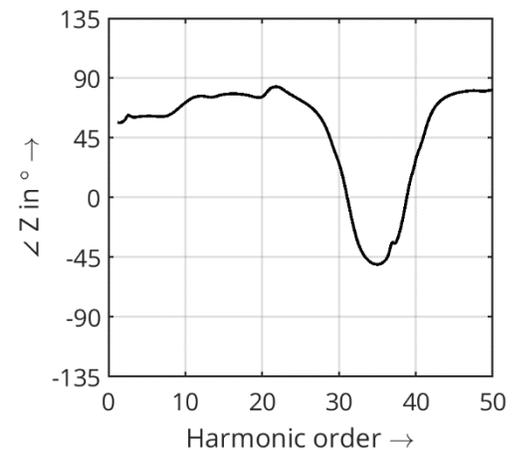
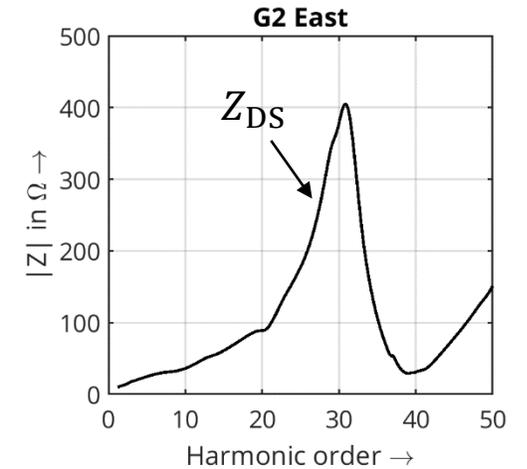


# Equivalent circuit models

## Circuit parameters (1)

### Estimation of circuit parameters

- Finding parameter values for defined circuit topology to fit downstream impedance  $Z_{DS}$
- Typical optimization problem for:
  - Nonlinear least squares
  - Constrained nonlinear multivariate functions
  - Particle swarm optimization
  - ...
- Limit search space for meaningful results (lower and upper boundaries for parameters e.g.  $R = [0, 200] \Omega$ )
- May require initial parameters values (e.g. middle of search space  $R_0 = 100 \Omega$ )



# Equivalent circuit models

## Circuit parameters (2)

### Estimation of circuit parameters

- Finding parameter values for defined circuit topology to fit downstream impedance  $\underline{Z}_{DS}$
- Typical optimization problem for:
  - Nonlinear least squares
  - Constrained nonlinear multivariate functions
  - Particle swarm optimization
  - ...
- Limit search space for meaningful results (lower and upper boundaries for parameters e.g.  $R = [0, 200] \Omega$ )
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*RL series (IEEE Model 1)*

$$\underline{Z}_{EC}(s) = R + s \cdot L$$

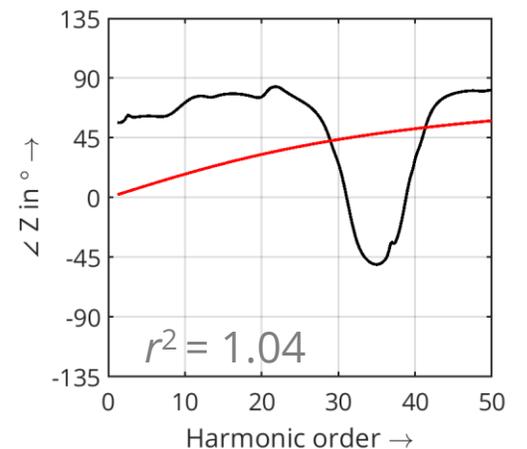
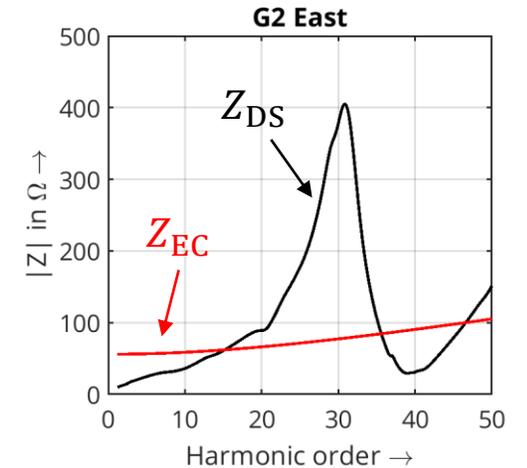
with  $s = j\omega = j2\pi f$

*Optimization function*

$$\min f(s) := \sum |\underline{Z}_{DS}(s) - \underline{Z}_{EC}(s)|^2$$

*Measure of fit*  
 ("normalized" R-squared)

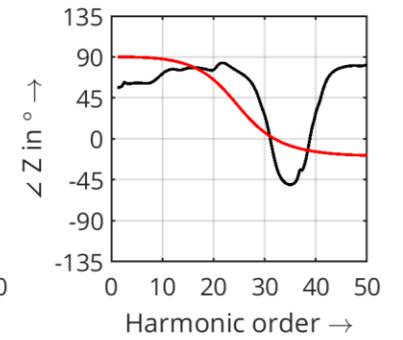
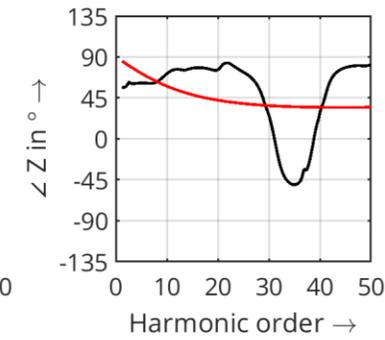
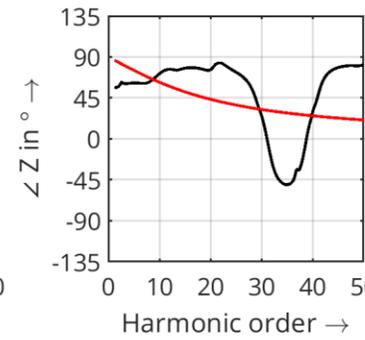
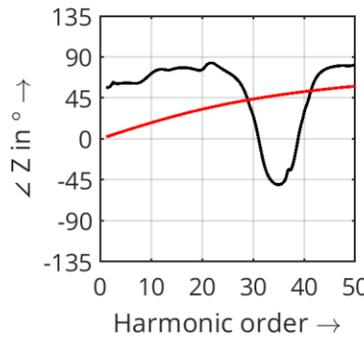
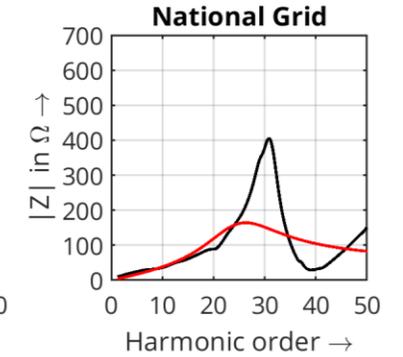
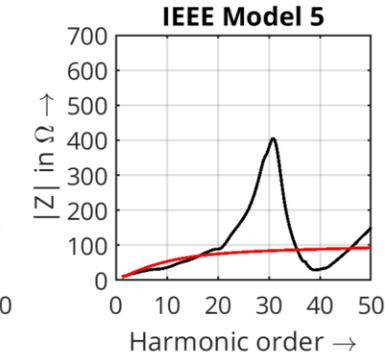
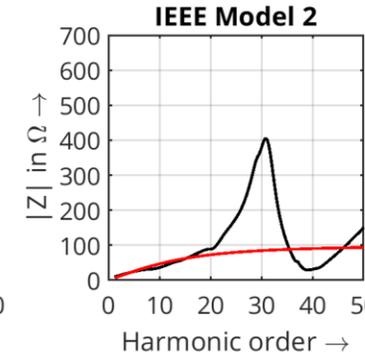
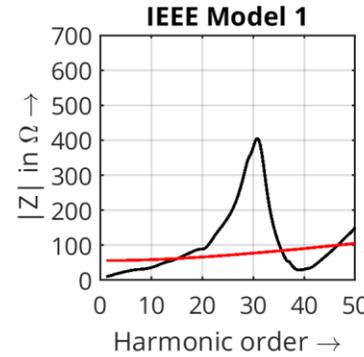
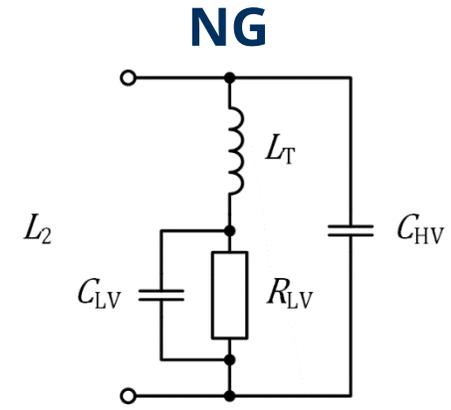
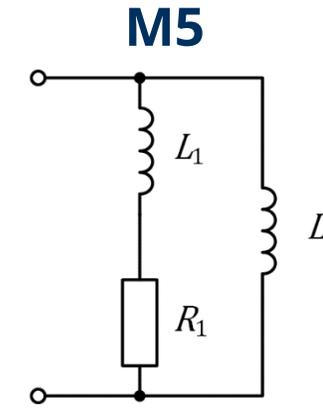
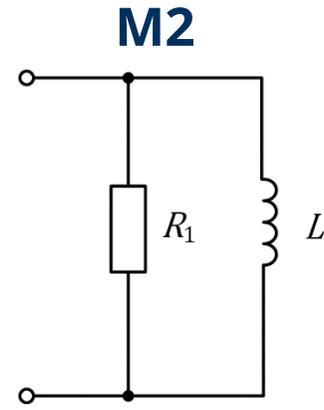
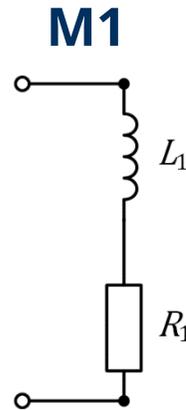
$$r^2 \approx \frac{\sum |\underline{Z}_{DS} - \underline{Z}_{EC}|^2}{\sum |\underline{Z}_{DS} - \bar{\underline{Z}}_{DS}|^2}$$



# Equivalent circuit models

## Circuit topologies (1)

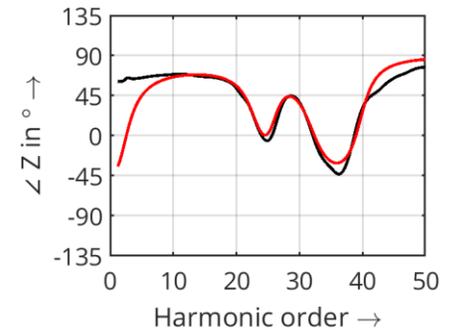
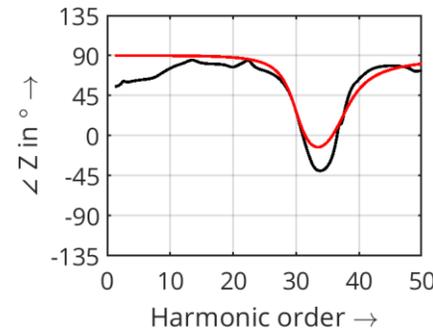
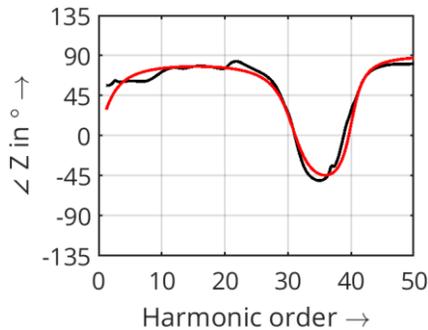
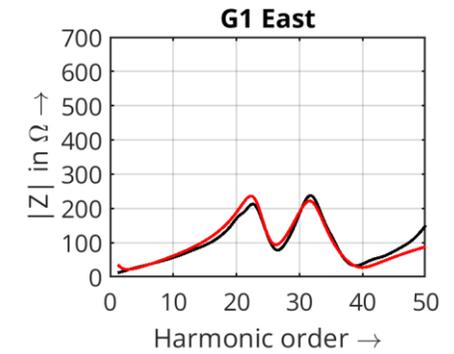
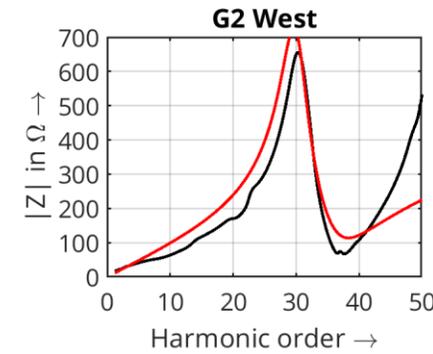
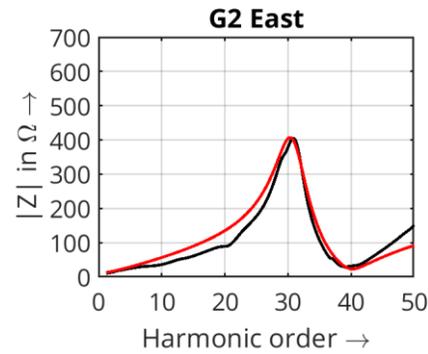
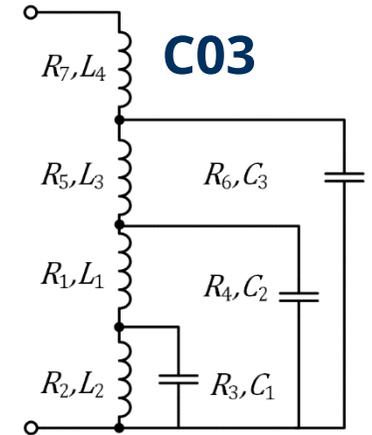
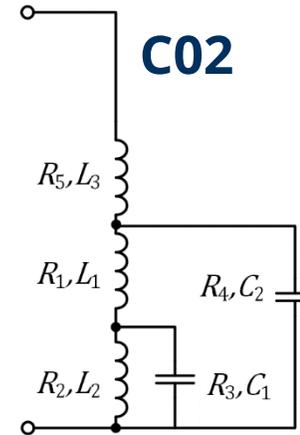
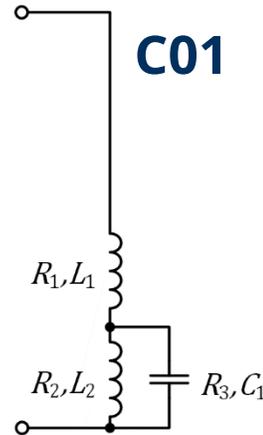
- Defining circuit topologies essential for the aggregated representation
- Conventional load models alone not suitable for (multiple) resonances



# Equivalent circuit models

## Circuit topologies (2)

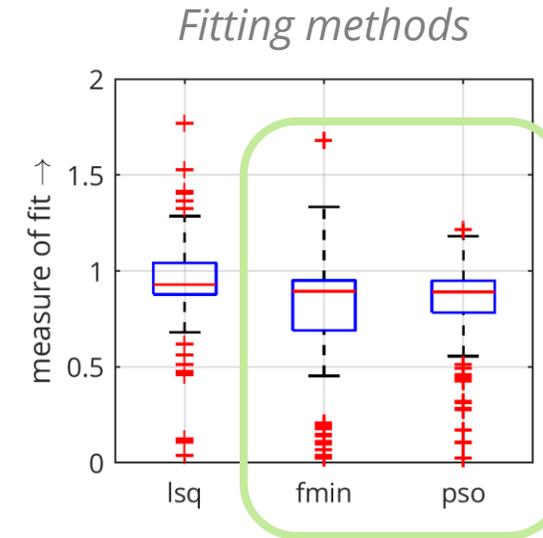
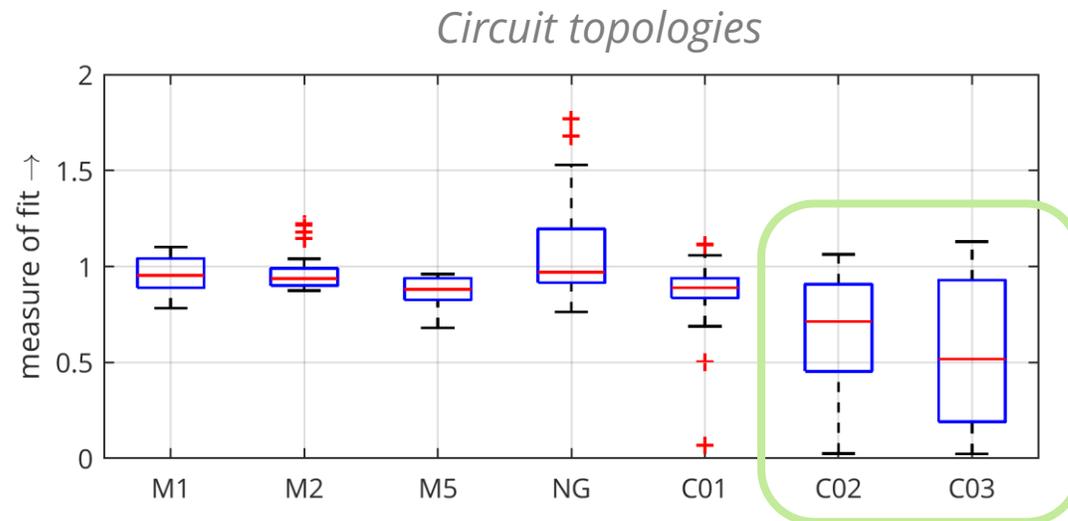
- Defining circuit topologies essential for the aggregated representation
- Conventional load models alone not suitable for (multiple) resonances
- Requires parallel and series resonant circuits:
  - C01 = 1x parallel/series resonances
  - C02 = 2x parallel/series resonances
  - C03 = 3x parallel/series resonances



# Equivalent circuit models

## Application results (1)

- Estimation of circuit parameters for different:
  - Fitting methods
  - Circuit topologies
  - Downstream impedances
  - Parameter search spaces
  - Initial parameter values



lsq ... Nonlinear least squares  
 fmin ... Constrained nonlinear multivariate functions  
 pso ... Particle swarm optimization

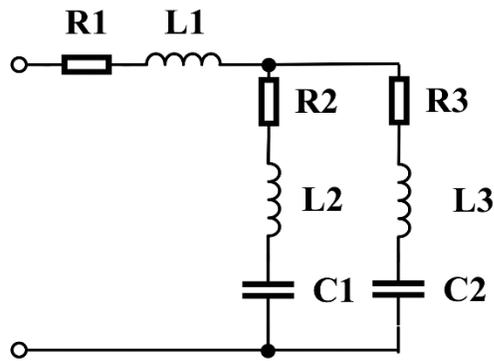
# Equivalent circuit models

## Application results (2)

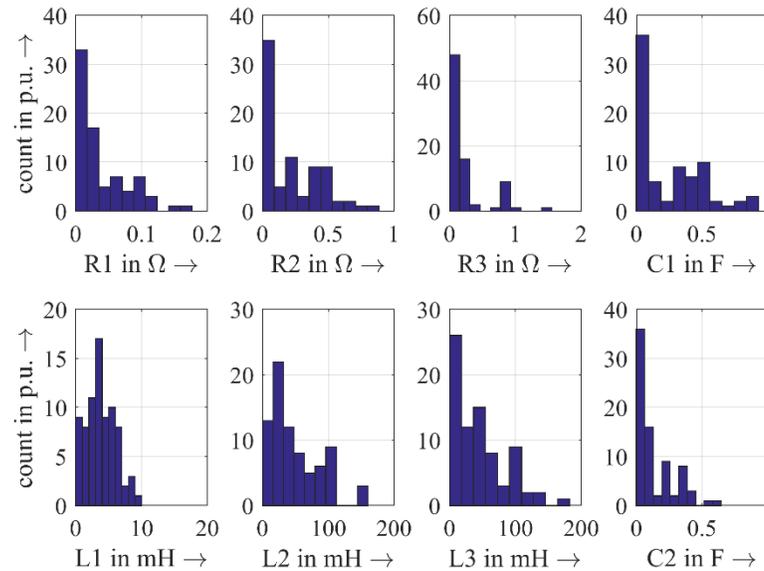
### Example application

- Fitting of **measured downstream LV impedances**
- Implementation for MV simulations
- Artificial increase of sample size by averaging parameters for combinations of fitted circuits

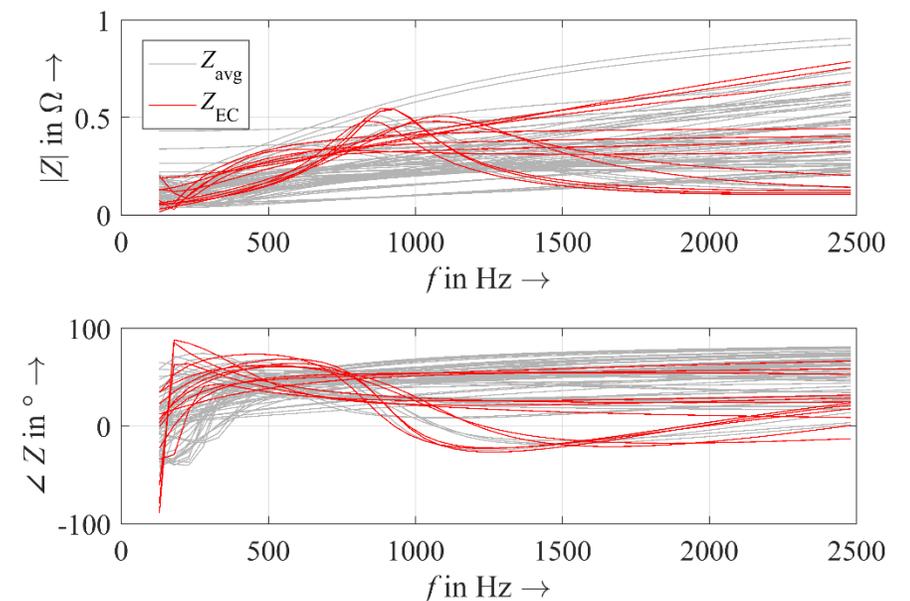
### *Optimal circuit topology*



### *Range of parameter values*



### *12 measured and 66 artificial impedances*



# Challenges

## Model fitting

### Selection of circuit topologies

- Modified load models
- Combinations of multiple load models

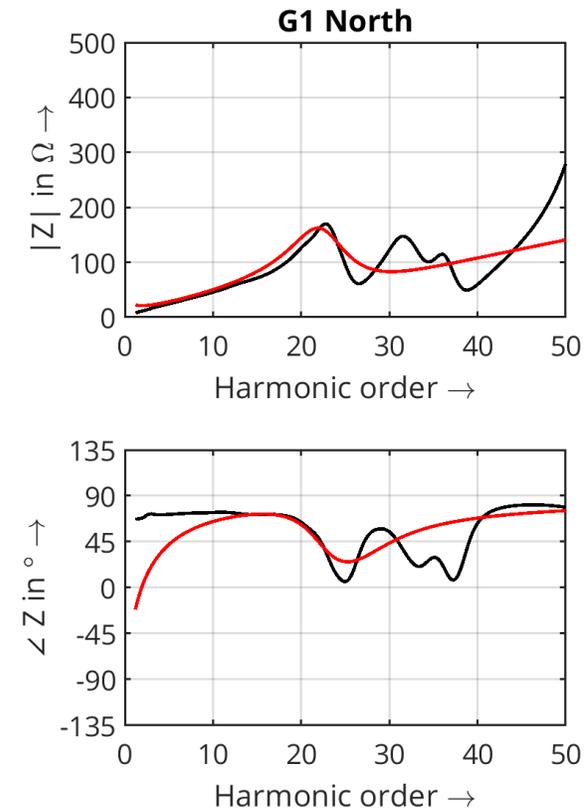
### Estimation of circuit parameters

- Parameter selective search spaces
- Additional constraints

### Alternative approaches

- Deduct circuit topologies from vector fitting results (e.g. number of poles  $\rightarrow$  resonances)

*Suboptimal fitting for multiple resonances*



# Challenges

## Model implementation

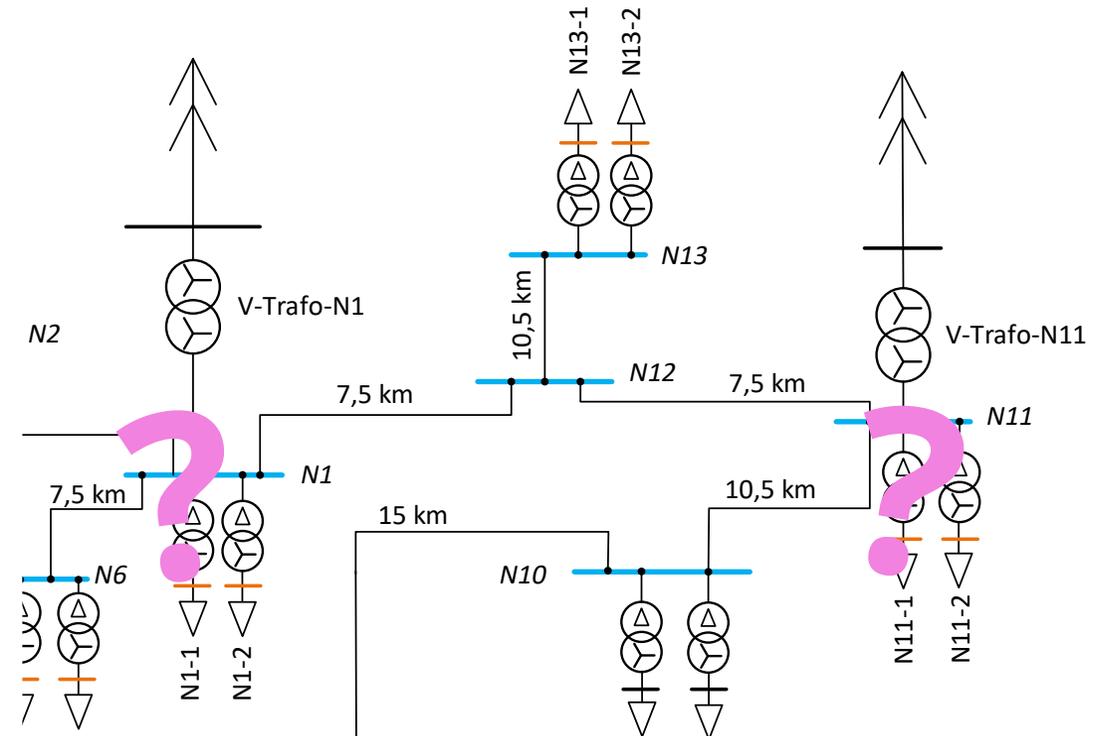
### Multiple in-feeds

- Individual equivalents per in-feed
- Determination of “meshed” equivalents

### Sequence systems

- Individual equivalents per sequence (positive, negative and zero sequence)
- Equivalents for coupled sequence systems (e.g. unbalanced conditions)

*Distribution network with multiple in-feeds*



# Thank you for your attention!



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